

Study Guide for the Quadratic Functions Quiz 2

LT4: Solve quadratic equations by factoring and graphing (4-5 Pg. 226)

Directions: Solve each of the following equations using factoring

1a.) $x^2 + 9x + 20 = 0$

1b.) $x^2 + 14x + 45 = 0$

2a.) $x^2 + 6x - 27 = 0$

$$\begin{array}{c} \wedge \\ 4 \quad 5 \\ (x+5)(x+4) = 0 \\ x+5=0 \quad x+4=0 \\ x=-5 \quad x=-4 \end{array}$$

$$\begin{array}{c} \wedge \\ 5 \quad 9 \\ (x+5)(x+9) = 0 \\ x+5=0 \quad x+9=0 \\ x=-5 \quad x=-9 \end{array}$$

$$\begin{array}{c} \wedge \\ +9 \quad -3 \\ (x+9)(x-3) = 0 \\ x+9=0 \quad x-3=0 \\ x=-9 \quad x=3 \end{array}$$

2b.) $x^2 - 7x + 18 = 0$

3a.) $2x^2 + 12x + 10 = 0$

3b.) $3x^2 + 14x + 8 = 0$

$$\begin{array}{c} \wedge \\ -9 \quad 2 \\ (x-9)(x+2) = 0 \\ x-9=0 \quad x+2=0 \\ x=9 \quad x=-2 \end{array}$$

$$\begin{array}{c} \wedge \\ 20 \\ 10 \quad 2 \\ (2x^2 + 10x)(2x + 10) = 0 \\ 2x(x+5) \quad 2(x+5) = 0 \\ 2x+2=0 \quad x+5=0 \\ x=-1 \quad x=-5 \end{array}$$

$$\begin{array}{c} \wedge \\ 24 \\ 12 \quad 2 \\ 3x^2 + 12x + 2x + 8 = 0 \\ 3x(x+4) + 2(x+4) = 0 \\ 3x+2=0 \quad x+4=0 \\ x=-\frac{2}{3} \quad x=-4 \end{array}$$

LT5: Solve quadratic equations using the quadratic formula (4-7 Pg. 240)

Directions: Find the discriminant of each of the equations and give the number of real solutions for each

4a.) $5x^2 + 7x - 9 = 0$

4b.) $x^2 - 5x + 7 = 0$

$$\begin{array}{l} a=5 \quad b=7 \quad c=-9 \\ b^2 - 4ac \\ 7^2 - 4(5)(-9) = 229 \end{array}$$

2 real solutions

$$\begin{array}{l} a=1 \quad b=-5 \quad c=7 \\ (-5)^2 - 4(1)(7) = -3 \end{array}$$

no real solutions

5a.) $3x^2 - 6x + 3 = 0$

5b.) $8x^2 + 3x - 7 = 0$

$$\begin{array}{l} (-6)^2 - 4(3)(3) \\ 36 - 36 = 0 \end{array}$$

1 real solution

$$\begin{array}{l} 3^2 - 4(8)(-7) \\ 9 + 224 = 233 \end{array}$$

2 real solutions

Directions: Solve each equation using the quadratic formula

6a.) $3x^2 + 5x - 8 = 0$

6b.) $x^2 - 6x + 9 = 0$

$$\begin{array}{l} \frac{-5 \pm \sqrt{5^2 - 4(3)(-8)}}{2(3)} \\ \frac{-5 \pm \sqrt{121}}{6} \\ \frac{-5+11}{6} = \frac{6}{6} = 1 \\ \frac{-5-11}{6} = \frac{-16}{6} = -\frac{8}{3} \end{array}$$

$$\begin{array}{l} \frac{6 \pm \sqrt{6^2 - 4(1)(9)}}{2(1)} \\ \frac{6 \pm \sqrt{0}}{2} \\ \frac{6 \pm 0}{2} = 3 \end{array}$$

7a.) $x^2 - 3x - 4 = 0$

7b.) $5x^2 + 7x - 6 = 0$

$$\begin{array}{l} x^2 - 3x - 4 = 0 \\ \frac{3 \pm \sqrt{3^2 - 4(1)(-4)}}{2(1)} \\ \frac{3 \pm \sqrt{25}}{2} \\ \frac{3+5}{2} = 4 \\ \frac{3-5}{2} = -1 \end{array}$$

$$\begin{array}{l} \frac{-7 \pm \sqrt{49 - 4(5)(-6)}}{10} \\ \frac{-7 \pm \sqrt{169}}{10} \\ \frac{-7+13}{10} = \frac{6}{10} = \frac{3}{5} \\ \frac{-7-13}{10} = -2 \end{array}$$

LT6: Identify, graph, and perform operations with complex numbers (4-8 Pg. 248)

Directions: Simplify each of the square roots below to write in terms of i

8a.) $\sqrt{-100}$
 $\sqrt{-1} \cdot \sqrt{100}$
 $10i$

8b.) $\sqrt{-25}$
 $\sqrt{-1} \sqrt{25}$
 $5i$

9a.) $3 + \sqrt{-81}$
 $3 + \sqrt{81} \sqrt{-1}$
 $3 + 9i$

9b.) $\sqrt{-4} + 8$
 $\sqrt{4} \sqrt{-1} + 8$
 $2i + 8$

10a.) $12 - \sqrt{-144}$
 $12 - \sqrt{144} \sqrt{-1}$
 $12 - 12i$

10b.) $\sqrt{-75} + 9$
 $\sqrt{25} \sqrt{3} \sqrt{-1} + 9$
 $5i\sqrt{3} + 9$

Directions: Solve each of the quadratic equations to find the complex conjugate (in terms of i)

11a.) $x^2 - 10x + 29 = 0$
 $\frac{10 \pm \sqrt{10^2 - 4(1)(29)}}{2(1)}$
 $\frac{10 \pm \sqrt{-16}}{2}$
 $\frac{10 \pm 4i}{2}$
 $5 \pm 2i$

11b.) $x^2 - 4x + 5 = 0$
 $\frac{4 \pm \sqrt{16 - 4(1)(5)}}{2(1)}$
 $\frac{4 \pm \sqrt{-4}}{2}$
 $\frac{4 \pm 2i}{2} \rightarrow 2 \pm i$

12.) $5x^2 - 6x + 9 = 0$
 $\frac{6 \pm \sqrt{(-6)^2 - 4(5)(9)}}{10}$
 $\frac{6 \pm \sqrt{-144}}{10}$
 $\frac{6 \pm 12i}{10} \rightarrow \frac{3}{5} \pm \frac{6}{5}i$

LT7: Solve and graph systems of equations involving quadratic functions (4-9 Pg. 258)

Directions: Solve each of the systems of equations below using either graphing or algebra.

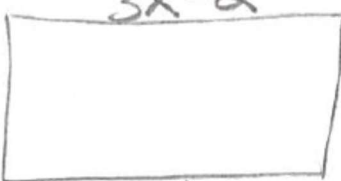
13.) $\begin{cases} y = x^2 - 10x + 12 \\ y = 2x + 12 \end{cases}$

graph (0, 12)
 (12, 36)

14.) $\begin{cases} y = 3x^2 - x + 1 \\ y = 3x^2 + x - 1 \end{cases}$

graph (1, 3)

BONUS: Jaylin is planning a rectangular garden. Its length is 2 ft less than three times its width. Its area is 65 ft². What are the dimensions of the garden?

$A = l \cdot w$

 length = 13 width = 5

$A = x(3x - 2) = 65$
 $3x^2 - 2x = 65$
 $\frac{-65 \quad -65}{3x^2 - 2x - 65 = 0}$
 graph
 $x = 5$
 $(5) \cdot 2 = 13$